

(GREEN TEXT) CHAPTER 2 NOTES – Equation Solving

Date:	
2.2 – Evaluation Expressions	
2.3 – Like Terms	
2.6 – Using Addition and Subtraction to Solve Equations	
2.7 – Using Division and Multiplication to Solve Equations	
2.10 – Solving Equations Using More than One Step	
2.11 – Solving Equations with Variables on Both Sides	
2.12 – The Distributive Property	
2.13 – Solving Equations with Brackets	
Review:	
Test:	<u> </u>

What You'll Learn:

- 2.2 using correct vocabulary to describe aspects of equations
- 2.3 strategies to add and subtract terms
- 2.6/2.7/2.10/2.11/2.13 strategies to solve equations of varying difficulty
- 2.12 how to correctly apply the distributive property

What is the opposite of each operation?

Operation	Opposite Operation
+	
-	+
X	÷
	×

What is an expression (may need to check glossary)?

O mathematical phrase that does not have an equals sign ex. 2π , 3x-5 What is an equation (may need to check glossary)?

a mathematical phrase that does have an 'equals' sign ex. x + 3 = 7

Warmup:

Name as many parts of the given expression as possible:

What is a variable?

What is a coefficient?

What is a term?

What is a constant?

What is an expression?

What is an equation?

What is substitution?

coefficient variable

a letter or symbol that represents an unknown or changing value ex. x, y, t

a number that multiplies a variable ex 2x (the big number in front of a variable) toofficient

a number, a variable, or the product of numbers and variables Terms are separated by t or -. -5y, 2, $2z^2yz$

a term in an expression or equation that is just a number ex In $2\pi-4$, -4 is the constant as it cannot change.

a mathematical phrase that does not have an 'equals' sign ex. $3x^2 - 2x + 7$

a mathematical phrase that does have an 'equals' sign ex $3x^2-2x+7=1$

A specific value is assigned to a variable in an expression or equation. Use brackets when substituting ex 3x + 5 when x = 1 3(1) + 5

ex1

Identify the

- a) variable(s)
- b) coefficient(s)
- c) constant(s)
- in each expression:

i)
$$2-7p$$

ii) $3x^2-y-5$

iii) x - 6b + 1

ex2

How many terms are in each question in

example 1?

ex3

Evaluate for x = -2

and y = 3

a)
$$xy + 2x$$

b)
$$3x^2 - 2y - 4$$

variables: x, y (ii) $3x^2 - y - 5$ Coefficients: 3, -1

Variables: x, b

coefficients: 1, -6

constant: 1

- (i) 2 terms
- (ii) 3 terms
- (iii) 3 terms.

(a)
$$xy + 2x$$

$$(-2)(3) + 2(-2)$$

(b)
$$3x^2 - 2y - 4$$

$$3(-2)^{2}-2(3)-4$$

Reflection: Try to make a commitment to use the correct vocabulary over the course of this chapter. What do you have to work at in order to make this happen?

Focus: To be able to identify, count, and combine applicable terms.

Main Ideas:

Warmup:

If you had 3 apples (3a) and 4 bananas (4b) in one bowl, and 2 apples (2a) and one banana (b) in a second bowl, and combined them, what would you have?

Answer in words but also show work using abbreviations given in brackets above.

Ex1

How many terms in each expression, and what are they?

a)
$$2x - 3y + 7$$

b)
$$x^2 - 6x + 4y - 1$$

What are like terms?

ex2

Simplify

- a) 7x + 10x + 3
- b) -9a + 2a
- c) 6m + 4 m
- d) 8x 1 + x 7
- e) 3xy 2y + x

5 apples and 5 bananas
5a and 5b

(a) 2x-3y+7: 3 terms 2x, -3y, 7

Terms with the same variable(s) raised to the same exponent (s)

ex. 2 and -5 3x and -2x $4x^2$ and x^2 3xy and 6xy

a) (7x)+10) + 2

(a) (7)(+10)(+3) (c)(6)(+4)(-1)(-1)

5m + 4 (e) 3xy - 2y + x no like terms

(b) (-9a) (+ 2a)

(d) 8) - [HZ] - 7 9x-8

a)
$$2m + n - 6 + n - 3m$$

b)
$$3x^2 - 4 + 2x - 3x^2 + x$$

c)
$$xy + 2xy^2 - 2xy$$

Ex4
Write the expression
$$2x - 3y + 5x^2 - 4$$

three other ways

(a)
$$2m+1n-6+1n-3m$$

- $m+2n-6$

(b)
$$3x^{2}-4+2x-3x^{2}+1x$$

 $3x-4$
(c) $1xy+2xy^{2}-2xy$

$$+2x-3y+5x^2-4$$

(i)
$$-3y + 5x^2 - 4 + 2x$$

many of the answers also

Reflection: Explain what 'like terms' are and how they're used for adding and subtracting.

Focus: Solving one-step equations using inverse operations.

Main Ideas:

Warmup:

Go to p.71 and answer #1, 5, 9, 12, 16, & 18 Write answers to the right:

What is 'solving by inspection'?

ex1 How do you solve x-2=8 algebraically?

Solving by inspection is when you solve an equation visually, without having to do any work on paper.

Think: 15 10-2 equal to 8? Questions to ask yourself:

(1) What is being done to z?

IT'S BEING SUBTRACTED BY 2

2) What's the opposite of that? To ADD 2

3 Do the opposite to both sides.

ADD 2 To BOTH SIDES.

(sides are separated by the equals sign)

What is the opposite of each operation?

Operation	Opposite Operation
+	_
_	+
X	÷
*	Χ

ex2 Solve n + 5 = 11algebraically. Ask yourself the relevant questions and show all work.

ex3 Solve & show work: a) y + 4 = -2

b) x - 7 = -1

c) 3 + p = 2

ex4 Solve & show work:

a) -4 + m = 6

b)
$$10 = -3 + x$$

N+5 = 11 What's being done to n?

Canully
$$-5$$
 | 11 5 is being done to n?

So is being ADDED to IT

South to opposite of that?

South to both sides

N = 6 (sides separated by equals' sign)

South to both sides

YES

(a) $y+y+f-2$ (b) $x-f=-1$ (c) $3+p=2$

rearrange left side

 $y=-6$
 y

Reflection: What are the questions you must ask yourself in order to solve an equation algebraically using inverse operations?

Warmup:

Solve y + 3 = 8algebraically and describe the questions you asked yourself throughout the process. Solve 3x = 27 using the same questions.

ex1 Solve by inspection and then algebraically:

$$2x = 6$$

ex2 – Solve and show work:

- a) 3y = -12
- b) -2w = -10
- c) 4 = -x
- d) 3 = 2m
- e) -2a = 0

$$y+3 \neq 8$$

Questions:

What is being clone to the variable?

 $y=5$

equal to 8? What is the opposite of that?

Yes

No it to both sides.

 $x=7$
 $x=$

Inspection:
2 times what is
equal to 6?

$$x = 3$$

Algebraically:
$$\frac{1}{2}x \neq \frac{6}{2}$$

Higheraically: What's being done to x?

17's BEING MULTIPLIED BY 2.

What's the opposite of that

TO DIVIDE BY 2 DIVIDE BY 2 TO BOTH SIDES.

(a)
$$3y = -12$$
 (c) $4 = -x$ (e) $-\frac{3y}{3} = -\frac{12}{3}$ $\frac{4}{-1} = \frac{1}{4}x$ $\frac{4}{-1} = -\frac{4}{4}x$ $\frac{4}{-1} =$

$$-2w = -10$$

$$-2w = -10$$

$$-2$$

$$-2$$

$$-2$$

$$-2$$

$$\frac{-4=x}{3=2m} = 0$$

$$\frac{3=2m}{2} = 0$$

- a) Do a 'check' for ex2a
- b) Do a check for ex2b

ex4 – Solve and check:

$$\frac{x}{2} = 4$$

ex5 – Solve & show work:

a)
$$\frac{y}{7} = 2$$

b)
$$\frac{m}{5} = -6$$

c)
$$-4 = \frac{x}{-3}$$

ex6
Do a check for 5b

$$3y = -12$$
 Chech: Left Side (LS) Right Side (RS)
 $y = -4$ Substitute $3(-4)$
 -12 Chech
works!

$$\frac{\chi}{2}$$
 = 4 What is being done to χ ?

IT'S BEING DIVIDED BY 2

What's the opposite?

 $\frac{\chi}{\chi}$ = 4(2) MULTIPLY BY 2

DO IT TO BOTH SIDES.

 $\frac{\chi=8}{2}$

(a)
$$\frac{4}{7} = 2$$
 (b) $\frac{100}{5} = -4.5$ (c) $\frac{12 - 2}{-3}$ (d) $\frac{12 - 2}{7} = 2.7$ (e) $\frac{12 - 2}{7} = 2.7$

$$\begin{array}{c|c} LS & RS \\ \hline \frac{M}{5} & -6 \\ \hline \begin{array}{c} -6 \\ \hline \end{array} \\ \hline \end{array}$$

Reflection: Describe the process for doing a check.

Warmup:

Solve 2x + 3 = 11 by inspection. What two things are happening to x? What is the opposite of each?

Ex1 - Solve2x + 3 = 11

Check your answer.

What are the steps to solving multi-step equations?

What number do you multiply by two and then add three to get 11? 2 = 4 - It is being multiplied by 2 → opp is to divide by 2 - It is being added by 3 > opp is to subtract 3. When solving equations, to the +/- first

$$2x + 3 = 11$$
 -3 subtract 3 to both sides
$$2x = 8$$

$$2x = \frac{8}{2}$$
 divide by 2 on both sides.
$$x = 4$$

$$\begin{array}{c|cccc}
L & & & & & & & \\
2x+3 & & & & & & \\
2(4)+3 & & & & & & \\
8+3 & & & & & & \\
11 & & & & & & \\
\end{array}$$

- 1.) Put together any like terms that are on the same side. 2.) What is happening to z?
- 3) What are the opposites?
- 4) Do the opposites to both sides, but do the add/sultract step first.
- 5.) Do the multiply /divide step. 6.) Check

$$ex2 - Solve$$
$$3x - 7 = 8$$

ex3 – Solve
a)
$$5x + 4 = -16$$

b) $3x + 2 + 2x = 7$
c) $-m + 3 = -2 - 6$

ex4 – Solve
a)
$$\frac{5x}{2} - 8 = -3$$

$$3x-1=8$$

$$x \text{ is being subtracted by 7 and } \frac{3x-1}{17}=8$$

$$x \text{ is being subtracted by 7 and } \frac{3x-1}{17}=7$$

$$x \text{ opposite is to add 7 and divide 3.}$$

$$x + \frac{15}{3}$$

a)
$$\frac{5x}{2} - 8 = -3$$

3 things happening to x
subtract $8 / \frac{div}{2} / \frac{div}{5} = -2y - 9p$: $\frac{18}{2} - \frac{1}{8} = -3$

$$\frac{5x}{2} - \frac{1}{8} = -3$$

$$\frac{-18}{2} = \frac{2y}{2}$$

$$\frac{5x}{2} = 5(2)$$

$$\frac{4x}{5} = \frac{10}{5}$$

$$\frac{1}{5} = \frac{10}{5}$$

$$\frac{1$$

Reflection: How will you go about solving multi-step equations so that you are certain that your answer is correct? Explain

Warmup:

For the equation 3x + 4 = 1 + 2x, how can you get the 2x term to the left side? Try your strategy, and then solve for x.

ex1 – Solve and jot down the questions you ask yourself

$$3x + 1 = x - 5$$

What are the steps when the variable is on both sides?

$$ex2$$
 – Solve and check $3x + 5x = -10 - 2x$

$$3x + 4 = 1 + 2\pi$$
 adding $2x$. What is opposite?
 $3x + 4 = 1 + 2\pi$ subtract $2x$ to both sides.
 $-2x - 7x$ subtract $2x$ to both sides.
 $-1x + 4 = 1$ or $x + 4 = 1$
 $-4 - 4$
 $x = -3$
 $3x + 1 = 1x - 5$ Then like terms on either side? No
 $-1x - 1x$ Thom do I get $1x$ to the left side?
 $1x + 1 = -5$ Then do I get $1x + 1 = 1$ to Both sides
 $1x + 1 = -5$ Then $1x + 1 = 1$ to Both sides
 $1x + 1 = -5$ Then $1x + 1 = 1$ to Both sides
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 $1x + 1 = 1$ to $1x + 1 = 1$ to $1x + 1 = 1$ to Both sides
 $1x + 1 = 1$ to $1x + 1 = 1$ to $1x + 1 = 1$ to $1x + 1 = 1$ to Both sides
 $1x + 1 = 1$ to 1

- 1) Combine any like terms on each side
- 2.) Get an x term to the other side so you're down to one x term.
- 3.) Ash what's happening to x?
- 4.) What's the opposite?
- 5.) Do the opposite to both sides doing add/subtract first

$$\begin{array}{llll}
3x + 5x &= -10 - 2x & \text{chech LS} & RS \\
8x &= -10 - 2x & 3x + 5z & -10 - 2x \\
+2z & +2z & 3(-1) + 5(-1) & -10 - 2(-1) \\
10x &= -10 & -3 + -5 & -10 + 2 \\
\hline
70 & 10 & -8 & -8 \\
7 &= -1
\end{array}$$

$$ex3$$
 – solve and check
 $3x + 2 = -3x - 16$

ex4 - Solve
$$4x - 7 + 2x = -20 - 5$$

$$ex5$$
 – Solve and check
 $3 + 2x = -x + 3 - 4x$

$$3x + 2 = -3k - 16$$

$$+3x + 4 = -16$$

$$5x + 4 = -16$$

$$6x + 4 = -16$$

$$-12 - 2$$

$$-1 + 2 = -18$$

$$2 = -3$$

$$4x - 7 + 2x = -25$$

$$6x - 7 = -25$$

$$17 + 17$$

$$6x = -18$$

$$6x = -1$$

 $\chi = 0$

Focus: To learn how to multiply a term into brackets.

Main Ideas:

ex1 - describe the steps
as you 'expand'
2(x + 5)

ex2 - Expand
a)
$$3(x + 2)$$

b) $7(x + 1)$
c) $-2(x + 6)$
d) $4(x - 4)$
e) $-(y - 3)$
f) $3(5x - 2y - 2)$

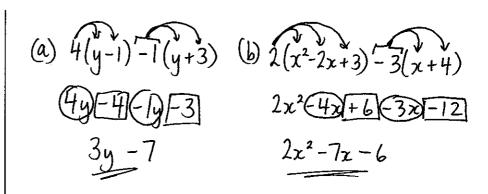
ex3 – Expand & Simplify
$$3(2x-3) - 3(2x-5)$$

$$3(2x-3) - 3(2x-5)$$

$$6x - 9 - 6x + 15$$

$$= 6$$

ex4 – Expand & Simplify a) 4(y-1) - (y+3)b) $2(x^2-2x+3) - 3(x+4)$



Reflection: What do you have to be most careful of when working with distributive property?

Write down the steps and solve the following equation:

$$2(x-3)-5=13-4x$$

$$ex1 - Solve & check$$

 $2(x-3) = 2$

$$ex2 - Solve & check$$

 $4(n + 7) = -44 + 2(n + 6)$

$$2(x-3)-5=13-4z$$

$$2x-6-5=13-4z$$

$$2x-11=13-4z$$

$$+4z + 4z$$

$$6x-11=13$$

$$+11+11$$

$$2(x-3)-5=13-4z$$

$$2x-6-5=13-4z$$

$$2x-11=13-4/z$$

$$+4z$$

$$6x-1/=13$$

$$\frac{6x}{7} = \frac{24}{6}$$

- (2) Combine like terms (same side only)
- B) Get variable to same side
 ADD 4x TO BOTH SIDE

 (F) What's happening to 2?
 SUBTRACT BY 11, MULT BY 6
- 6 What & the opposite? ADD BY 11, DIV BY 6

$$2(x-3) = 2$$

 $2x-4 = 2$
 $+6 + 6$

$$\frac{2x = 8}{2}$$

$$x = 4$$

$$4(n+7) = -44 + 2(n+6)$$

 $4n + 28 = -44) + 2n (+12)$

$$4n + 28 = -32 + 2h$$

-2n -2n

$$2n + 28 = -32$$

 -28 -28

$$\frac{1}{2}n = \frac{-60}{2}$$

ex3 – Solve

$$7(x-1)-2(x-6) = 2(x-5)+6$$

ex4 - Solve
$$2(x+1) - (x+4) = 1$$

$$7(x-1)-2(x-6) = 2(x-5)+6$$

$$7x-7-2x+12 = 2x-10x+6$$

$$5x+5 = 2x-4$$

$$-2x - 2x$$

$$3x+5 = -4$$

$$-5 - 5$$

$$\frac{3}{3}x = -\frac{9}{3}$$

$$\frac{x=-3}{3}$$

$$\frac{x=-3}{2(x+1)-1(x+4)=1}$$

$$2x+2-12-14=1$$

$$x-2=1$$

$$+2+2$$

$$x=3$$

Reflection: Write the general steps in your words for solving an equation like that in ex4.